Trigonometry Review

Show your work and draw a diagram for each word problem

1. Use your calculator to determine the trigonometric ratio for each angle to four decimal places.
   a) $\sin 33^\circ = 0.5446$
   b) $\tan 50^\circ = 1.1918$
   c) $\cos 3^\circ = 0.9986$
   d) $\sin 68^\circ = 0.9272$

2. Calculate the length of the missing side $x$.
   a) $\cos 59^\circ = \frac{x}{6.0} \quad x = 6.0 \cos(59^\circ) \quad x = 3.09$
   b) $\tan(45^\circ) = \frac{3.0}{x} \quad x = \frac{3}{\tan(45^\circ)} \quad x = 3$
   c) $\cos 63^\circ = \frac{x}{15} \quad x = 15 \cos 63^\circ \quad x = 6.8$ cm
   d) $\cos 42^\circ = \frac{y}{2.4} \quad y = \frac{2.4}{\cos 42^\circ} \quad y = 3.23$

3. Find the missing angle to the nearest degree.
   a) $\tan(b) = \frac{45}{38} \quad b = \tan^{-1}(1.1842) \quad b = 50^\circ$
   b) $\cos x = \frac{3.5}{9} \quad x = 69^\circ$
4. Solve \( \triangle PQR \), where \( \angle Q = 90^\circ \), \( PR = 5.1 \text{ cm} \) and \( PQ = 2.8 \text{ cm} \).

\[
\cos P = \frac{2.8}{5.1} \quad \sin(57^\circ) = \frac{x}{5.1} \\
\angle P = 57^\circ \\
\angle R = 180^\circ - 90^\circ - 57^\circ \\
\angle R = 33^\circ \\
x = 5.1 \sin(57^\circ) \\
x = 4.3 \text{ cm}
\]

5. How high is a weather balloon tied to the ground if it is attached to a 15 m string, and the angle between the string and the ground is 35°?

\[
\sin 35^\circ = \frac{x}{15} \\
x = 15 \sin 35^\circ \\
x = 8.6 \text{ m}
\]

6. Two guy wires of unequal lengths keep this flagpole vertical. Both wires are attached 3 m from the top of the pole.

a) What is the height of the pole, to the nearest metre?

\[
\tan(51) = \frac{h}{8.6} \\
h = 8.6 \tan 51^\circ \\
h = 10.6 \text{ m}
\]

b) The other wire is attached on the ground, 8.6 m from the pole. What is the length of this wire?

\[
\cos(51) = \frac{8.6}{y} \\
y = \frac{8.6}{\cos(51)} \\
y = 13.7 \text{ m}
\]
7. Simon is training new employees on ladder safety. For safety reasons, the ladder needs to make an angle of 75° with the ground. If you set up a ladder that is 12 ft long, how far from the base of the wall should you set it up?

\[
\sin(75^\circ) = \frac{x}{12}
\]

\[x = 12 \sin(75^\circ)\]

\[x = 11.6\]

8. A flagpole casts a shadow that is 5 m long. Jim looks at the shadow and at the flagpole. He thinks they are about the same length. If Jim is correct, at what angle are the sun’s rays hitting the ground?

\[\tan x = \frac{5}{5}\]

\[x = \tan^{-1}(1)\]

\[x = 45^\circ\]

9. A cable is 19 m long. It supports a utility pole that is 15 m tall.

a) Determine the measure of the angle that the cable forms with the ground.

\[\sin x = \frac{15}{19}\]

\[x = 52^\circ\]

b) Calculate the distance from the base of the pole to the point where the cable meets the ground using the Pythagorean Theorem.

\[a^2 + 15^2 = 19^2\]

\[a^2 = 361 - 225\]

\[a^2 = 136\]

\[a = 11.7\]
10. Upon takeoff, an airplane climbs at a $7^\circ$ angle of elevation. After the plane has travelled 5 km along its flight path, how high is the plane?

\[ \sin 7^\circ = \frac{x}{5} \]

\[ x = 5 \cdot \sin 7^\circ \]

\[ x = 0.61 \text{ km} \]

11. Two office towers are 50 m apart. From the top of the shorter tower, the angle of elevation to the top of the taller tower is $20^\circ$. The angle of depression to the base of the taller tower is $35^\circ$. Determine the height of each tower.

\[ \tan 20^\circ = \frac{x}{50} \]

\[ x = 50 \tan 20^\circ \]

\[ x = 18 \]

\[ \tan 35^\circ = \frac{y}{50} \]

\[ y = 50 \tan 35^\circ \]

\[ y = 35 \]

**tall tower 53 m**

**shorter tower 18 m**

12. A ship travels due west for 550 km then travels on a bearing of $40^\circ$ until it is directly north of its starting point. What is the total distance the ship has travelled?

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13. A popular tourist attraction in Ottawa is the Peace Tower, which rises from the centre block of the Parliament Buildings. A mast stands on top of the tower. From a point 25 m away from the base of the tower, the angle of elevation to the top of the tower is $74.8^\circ$. From the same point, the angle of elevation to the top of the mast is $76.3^\circ$. Find the height of the mast.

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