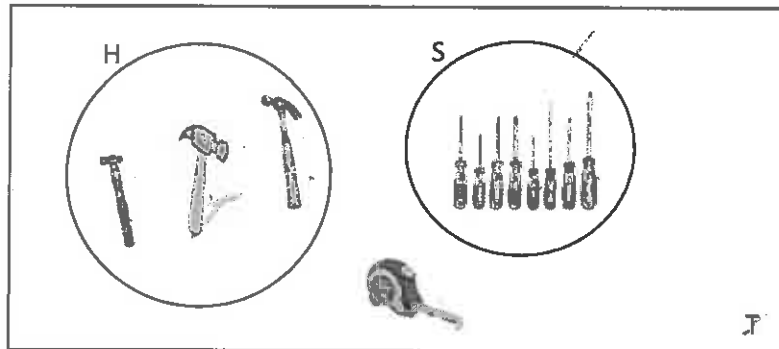


In set theory, Venn diagrams are often used to show the relationship between sets and their subsets.

### Example 1

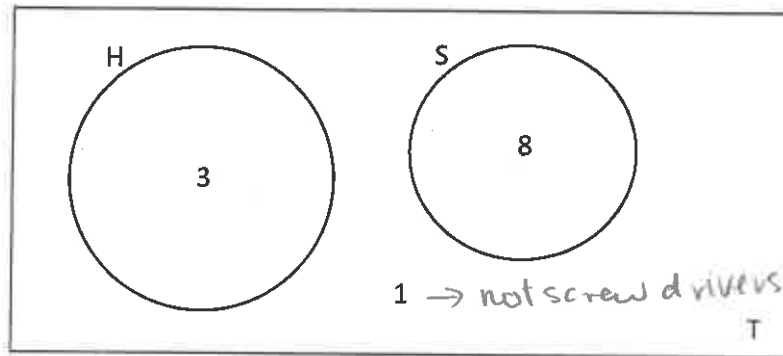
Suppose Claire has a set of tools,  $T$ , which consists of 3 hammers, 8 screwdrivers, and a measuring tape. Notice that the subsets have been represented by circles within the universal set  $T$ . Also note that the position and size of the circles does not matter – they are just a visual to help differentiate one subset from another.



- a) Use set notation to complete the last column of the following table. The first one is done for you.

the number of elements in the universal set of tools, $T$ , is 12	$n(T) = 12$
the set of screw drivers, $S$ , is a subset of the universal set, $T$	$S \subset T$
the number of elements in the subset, $S$ , is 8	$n(S) = 8$
the number of elements in the set of hammers, $H$ , is 3	$n(H) = 3$
The set of hammers is a subset of the universal set $T$	$H \subset T$

- b) The following Venn diagram shows the number of elements in the universal set T and in the subsets H and S.



S = screw drivers  
 H = hammers  
 T = tools

1 → not screw drivers or hammers  
 $n(H' \cup S') = 1$

Determine the following:

i)  $n(H) = 3$

ii)  $n(S) = 8$

iii)  $n(T) = 12$

$n(H)$  → means, number of elements in subset H

$n(S)$  - number of elements in subsets

- c)  $H'$  means "not in set H".  
 $H'$  is read as "H prime".

$H'$  is called the **complement of H**. - do not belong to H

Determine the following:

i)  $n(H') = 9$  → not hammer

ii)  $n(S') = 4$  → not screw drivers

$n(H')$  How many elements in the set that are NOT hammers

**Example 2**

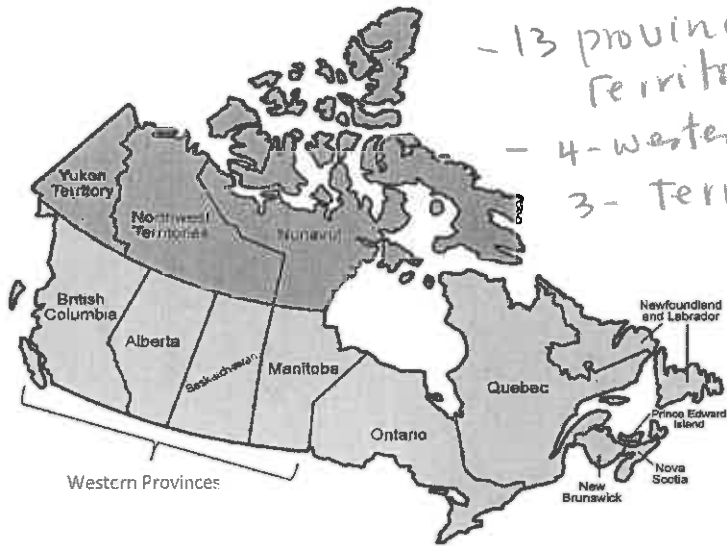
Use the map of Canada and the following information to answer the questions.

$C = \{\text{All the provinces and territories of Canada}\}$

$W = \{\text{Western provinces}\}$

$T = \{\text{Territories}\}$

Determine the following:



a)  $n(C) = 13$

b)  $n(W) = 4$

c)  $n(T) = 3$

d) List the elements of set W.   
 - Provinces   
 { BC, Alberta, Saskatchewan, Manitoba }

e) List the elements of W'.   
 name (NOT Western provinces)   
 { YT, NWT, NU, ON, QC, NB, NS, PEI, NL }

f) Determine  $n(W')$ .   
 number  $= 9$

g) Is T a subset of C? Explain.   
 Yes. Because the territories are within Canada

h) Is T a subset of W? Explain.   
 Not in Western Canada   
 No, the territories are not in Western Canada

i) Is W' a subset of C?   
 (OWTAR... is a subset) Yes!

j) Is T a subset of W'?   
 on T, Yes - The territories are part of the other non-western provinces

k) Are T and W disjoint sets? Explain.

Yes, because T - territories   
 W - Provinces   
 are separate subsets   
 Disjoint sets have no elements in common.

l) Let set S be defined as the set of Canadian provinces south of Mexico. What is unusual about this set?

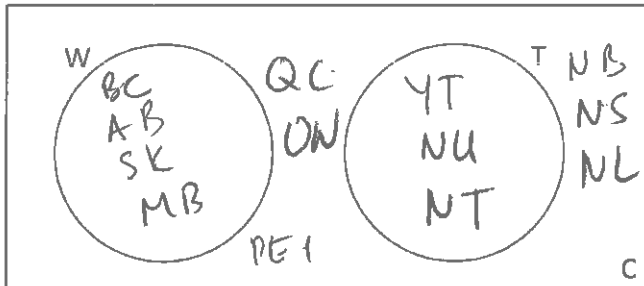
A set with no elements is called an **empty set**. Symbols used include  $\{\}$  or  $\emptyset$ .

no Canadian provinces south of Mexico  $\{\}$  or  $\emptyset$

Abbreviations
AB
BC
MB
NB
NL
NS
NT
NU
ON
PE
QC
SK
YT

(example 2 continued...)

- m) Place the abbreviation for each Canadian province or territory in the correct part of the Venn diagram below.



(notice that since the sets  $W$  and  $T$  are *disjoint*, the circles do not overlap)

### Example 3

- a) Complete each of the following statements to show the members of each set.

Universal Set

$$U = \{ \text{set of whole numbers from } \underline{1} \text{ to } \underline{10} \}$$

$$= \{ 1, 2, 3, 4, 5, 6, 7, 8, 9, 10 \}$$

Subsets

$$E = \{ \text{set of even numbers less than } 10 \}$$

$$= \{ 2, 4, 6, 8 \}$$

$$O = \{ \text{set of odd numbers less than } 10 \}$$

$$= \{ 1, 3, 5, 7, 9 \}$$

$$P = \{ \text{set of prime numbers less than or equal to } 10 \}$$

$$= \{ 1, 2, 3, 5, 7 \}$$

$$M = \{ \text{multiples of } 4 \}$$

$$= \{ 4, 8 \}$$

- b) Use set notation to indicate which of the above sets are subsets.

$$O \subset U, P \subset U, M \subset U,$$

$$M \subset E$$

$C$  subset

## Example 4

- a) Given the Universal Set  $U = \{\text{all integers from 1 to 20}\}$  show the elements of the following sets, using set notation.

1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15,  
16, 17, 18, 19, 20

$$F = \{\text{multiples of 5 from 1 to 20}\}$$

$$= \{5, 10, 15, 20\}$$

$$A = \{\text{multiples of 3 from 1 to 20}\}$$

$$\{3, 6, 9, 12, 15, 18\}$$

$$S = \{\text{all multiples of 7 from 1 to 20}\}$$

$$\{7, 14\}$$

$$T = \{\text{multiples of 10 from 1 to 20}\}$$

$$\{10, 20\}$$

- b) Is each of the following statements true or false? Justify your answers.

i)  $F \subset T$  False.  $\rightarrow$  All <sup>(numbers)</sup> elements in  $F$  are NOT in  $T$   
 $\downarrow$   
 $\{5, 10, 15, 20\}$   $\{10, 20\}$

ii)  $T \subset F$  True. The <sup>(numbers)</sup> elements in  $T$   $\{10, 20\}$  are in  $F$   $\{5, 10, 15, 20\}$

iii)  $F \subset U$  True. All numbers in  $F$   $\{5, 10, 15, 20\}$  are in the universal set  $\{1, \dots, 20\}$

iv)  $F' = \{\text{multiples of 10 from 1 to 20}\}$  False - There are other numbers from 1 to 20 that are not multiples of 10.  $\rightarrow 1, 2, 3, \dots$   
 $\swarrow$   
 Not multiples of 5  
 NOT  $\{5, 10, 15, 20\}$

- v) For this example, the set of integers from 21 to 30 is  $\{ \}$ .

$\uparrow$  empty set  
 This is true. there are no numbers in the set that are between 21 and 30