

## Lesson 5.2 Exercises, pages 360–368

### A

3. Determine whether each point is a solution of the given inequality.

a)  $3x - 2y \geq -16$     A(-3, 4)

In the inequality, substitute:  $x = -3, y = 4$

L.S.:  $3(-3) - 2(4) = -17$     R.S. =  $-16$

Since the L.S. < R.S., the point is not a solution.

b)  $4x - y \leq 5$     B(-1, 1)

In the inequality, substitute:  $x = -1, y = 1$

L.S.:  $4(-1) - 1 = -5$     R.S. =  $5$

Since the L.S. < R.S., the point is a solution.

c)  $3y > 2x - 7$     C(-2, -5)

In the inequality, substitute:  $x = -2, y = -5$

L.S.:  $3(-5) = -15$     R.S.:  $2(-2) - 7 = -11$

Since the L.S. < R.S., the point is not a solution.

d)  $5x - 2y + 8 < 0$     D(6, 7)

In the inequality, substitute:  $x = 6, y = 7$

L.S.:  $5(6) - 2(7) + 8 = 24$     R.S. =  $0$

Since the L.S. > R.S., the point is not a solution.

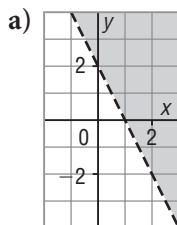
4. Match each graph with an inequality below.

i)  $2x + y \leq -2$

ii)  $2x + y > 2$

iii)  $x - 2y < 2$

iv)  $x - 2y \geq -1$

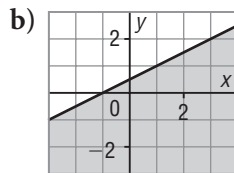


The line has slope  $-2$  and  $y$ -intercept  $2$ , so its equation is:

$y = -2x + 2$ , or  $2x + y = 2$

The inequality is:

$2x + y > 2$

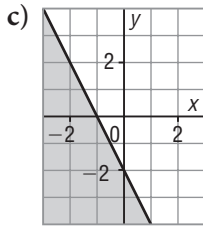


The line has slope  $0.5$  and  $y$ -intercept  $0.5$ , so its equation is:

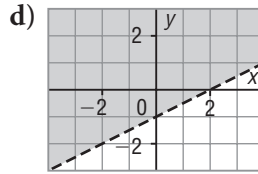
$y = 0.5x + 0.5$ , or  $x - 2y = -1$

The inequality is:

$x - 2y \geq -1$

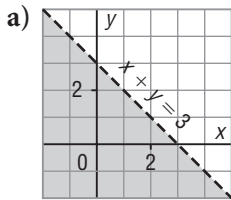


The line has slope  $-2$  and  $y$ -intercept  $-2$ , so its equation is:  
 $y = -2x - 2$ , or  $2x + y = -2$   
 The inequality is:  
 $2x + y \leq -2$

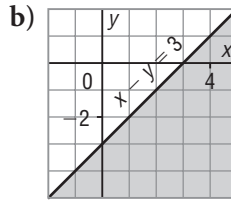


The line has slope  $0.5$  and  $y$ -intercept  $-1$ , so its equation is:  
 $y = 0.5x - 1$ , or  $x - 2y = 2$   
 The inequality is:  
 $x - 2y < 2$

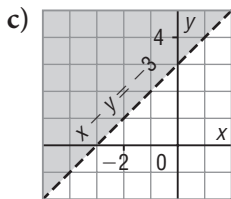
5. Write an inequality to describe each graph.



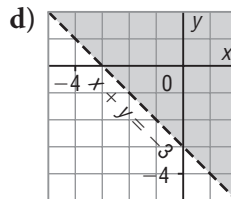
The equation can be written as:  $y = -x + 3$   
 The line is broken, and the shaded region is below the line so an inequality is:  $y < -x + 3$ , or  $x + y < 3$



The equation can be written as:  $y = x - 3$   
 The line is solid, and the shaded region is below the line so an inequality is:  $y \leq x - 3$ , or  $x - y \geq 3$



The equation can be written as:  $y = x + 3$   
 The line is broken, and the shaded region is above the line so an inequality is:  $y > x + 3$ , or  $x - y < -3$

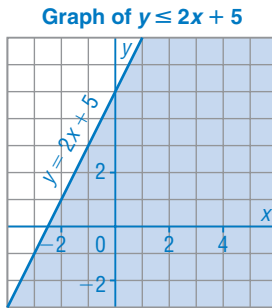


The equation can be written as:  $y = -x - 3$   
 The line is broken, and the shaded region is above the line so the inequality is:  $y > -x - 3$ , or  $x + y > -3$

**B**

6. Graph each linear inequality.

a)  $y \leq 2x + 5$



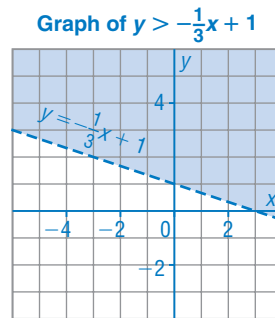
Use intercepts to graph the related functions.

When  $x = 0$ ,  $y = 5$

When  $y = 0$ ,  $x = -2.5$

Draw a solid line. Shade the region below the line.

b)  $y > -\frac{1}{3}x + 1$

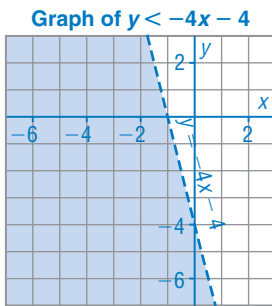


When  $x = 0$ ,  $y = 1$

When  $y = 0$ ,  $x = 3$

Draw a broken line. Shade the region above the line.

c)  $y < -4x - 4$



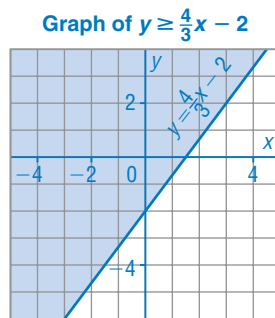
Use intercepts to graph the related functions.

When  $x = 0$ ,  $y = -4$

When  $y = 0$ ,  $x = -1$

Draw a broken line. Shade the region below the line.

d)  $y \geq \frac{4}{3}x - 2$



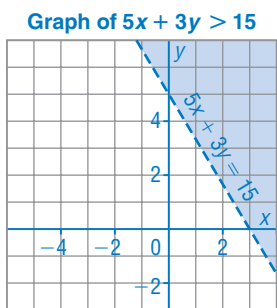
When  $x = 0$ ,  $y = -2$

When  $y = 0$ ,  $x = 1.5$

Draw a solid line. Shade the region above the line.

7. Graph each linear inequality. Give the coordinates of 3 points that satisfy the inequality.

a)  $5x + 3y > 15$



Use intercepts to graph the related functions.

When  $x = 0$ ,  $y = 5$

When  $y = 0$ ,  $x = 3$

Use  $(0, 0)$  as a test point.

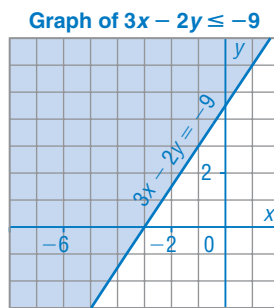
L.S. = 0; R.S. = 15

Since  $0 < 15$ , the origin does not lie in the shaded region.

Draw a broken line. Shade the region above the line.

From the graph, 3 points that satisfy the inequality are:  $(2, 3)$ ,  $(1, 5)$ ,  $(3, 2)$

b)  $3x - 2y \leq -9$



When  $x = 0$ ,  $y = 4.5$

When  $y = 0$ ,  $x = -3$

Use  $(0, 0)$  as a test point.

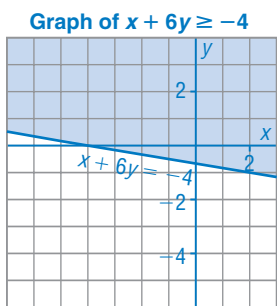
L.S. = 0; R.S. = -9

Since  $0 > -9$ , the origin does not lie in the shaded region.

Draw a solid line. Shade the region above the line.

From the graph, 3 points that satisfy the inequality are:  $(-2, 3)$ ,  $(-1, 4)$ ,  $(-1, 6)$

c)  $x + 6y \geq -4$



Graph the related functions.

When  $y = 0$ ,  $x = -4$

When  $y = -1$ ,  $x = 2$

Use  $(0, 0)$  as a test point.

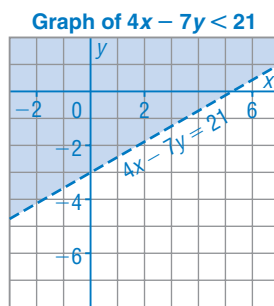
L.S. = 0; R.S. = -4

Since  $0 > -4$ , the origin lies in the shaded region.

Draw a solid line. Shade the region above the line.

From the graph, 3 points that satisfy the inequality are:  $(2, 1)$ ,  $(1, 2)$ ,  $(3, 3)$

d)  $4x - 7y < 21$



When  $x = 0$ ,  $y = -3$

When  $y = 1$ ,  $x = 7$

Use  $(0, 0)$  as a test point.

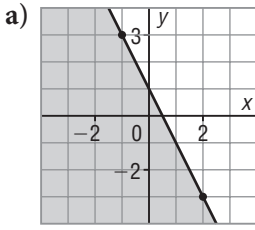
L.S. = 0; R.S. = 21

Since  $0 < 21$ , the origin lies in the shaded region.

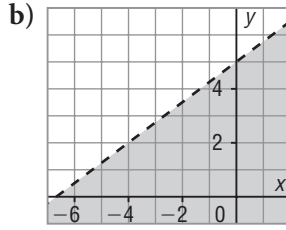
Draw a broken line. Shade the region above the line.

From the graph, 3 points that satisfy the inequality are:  $(-1, 3)$ ,  $(1, -1)$ ,  $(2, 3)$

8. Write an inequality to describe each graph.



The line has slope  $-2$  and  $y$ -intercept  $1$ , so its equation is:  $y = -2x + 1$   
 The line is solid and the region below is shaded.  
 An inequality is:  
 $y \leq -2x + 1$



The line has slope  $\frac{3}{4}$  and  $y$ -intercept  $5$ , so its equation is:  $y = \frac{3}{4}x + 5$   
 The line is broken and the region below is shaded.  
 An inequality is:  
 $y < \frac{3}{4}x + 5$

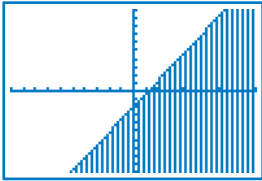
9. A student graphed the inequality  $2x - y < 0$  and used the origin as a test point. Could the student then shade the correct region of the graph? Explain your answer.

No, the line passes through the origin, so it cannot be used as a test point. The test point must not lie on the line that divides the region.

10. Use technology to graph each linear inequality. Sketch the graph.

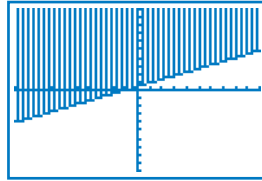
a)  $y < 1.6x - 1.95$

Graph:  $y = 1.6x - 1.95$   
 The boundary is not part of the graph.



b)  $y > \frac{4}{9}x + \frac{3}{7}$

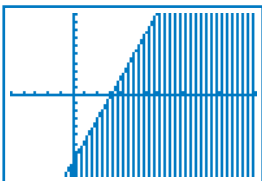
Graph:  $y = \frac{4}{9}x + \frac{3}{7}$   
 The boundary is not part of the graph.



c)  $8x - 3y - 25 \geq 0$

$3y \leq 8x - 25$   
 $y \leq \frac{8}{3}x - \frac{25}{3}$   
 Graph:  $y = \frac{8}{3}x - \frac{25}{3}$

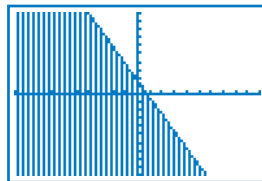
The boundary is part of the graph.



d)  $4.8x + 2.3y - 3.7 \leq 0$

$2.3y \leq -4.8x + 3.7$   
 $y \leq \frac{-4.8}{2.3}x + \frac{3.7}{2.3}$   
 Graph:  $y = \frac{-4.8}{2.3}x + \frac{3.7}{2.3}$

The boundary is part of the graph.



- 11.** Nina takes her friends to an ice cream store. A milkshake costs \$3 and a chocolate sundae costs \$2.50. Nina has \$18 in her purse.
- a) Write an inequality to describe how Nina can spend her money.

Let  $m$  represent the number of milkshakes and  $s$  represent the number of sundaes.

An inequality is:  $3m + 2.5s \leq 18$

- b) Determine 3 possible ways Nina can spend up to \$18.

Determine the coordinates of 2 points that satisfy the related function.

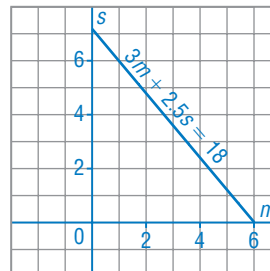
When  $s = 0$ ,  $m = 6$

When  $s = 6$ ,  $m = 1$

Join the points with a solid line.

The solution is the points, with whole-number coordinates, on and below the line.

Three ways are: 4 milkshakes, 2 sundaes; 3 milkshakes, 3 sundaes; 2 milkshakes, 4 sundaes



- c) What is the most money Nina can spend and still have change from \$18?

The point, with whole-number coordinates, that is closest to the line has coordinates (5, 1); the cost, in dollars, is:

$$(5)(3) + 1(2.50) = 17.50$$

Nina can spend \$17.50 and still have change.

- 12.** The relationship between two negative numbers  $p$  and  $q$  is described by the inequality  $p - 2q > -6$ .

- a) What are the restrictions on the variables?

Since the numbers are negative,  $p < 0$  and  $q < 0$

- b) Graph the inequality.

Determine the coordinates of 2 points that satisfy the related function.

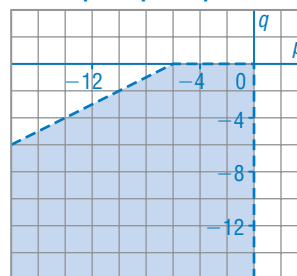
When  $p = -10$ ,  $q = -2$

When  $p = -6$ ,  $q = 0$

Draw a broken line through the points.

The solution is the points below the line in Quadrant 3.

Graph of  $p - 2q > -6$



- c) Write the coordinates of 2 points that satisfy the inequality.

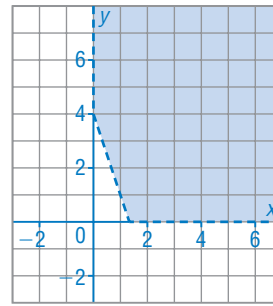
Sample response: Two points are:  $(-4, -4)$  and  $(-12, -4)$

**13.** Graph each inequality for the given restrictions on the variables.

a)  $y > -3x + 4$ ; for  $x > 0, y > 0$

Since  $x > 0, y > 0$ , the graph is in Quadrant 1.  
 The graph of the related function has slope  $-3$  and  $y$ -intercept  $4$ .  
 Draw a broken line to represent the related function in Quadrant 1.  
 Shade the region above the line.  
 The axes bounding the graph are broken lines.

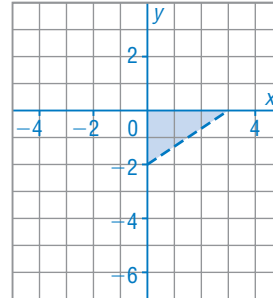
Graph of  $y > -3x + 4$ ,  
 $x > 0, y > 0$



b)  $2x - 3y < 6$ ; for  $x \geq 0, y \leq 0$

Since  $x \geq 0, y \leq 0$ , the graph is in Quadrant 4.  
 Graph the related function.  
 When  $y = 0, x = 3$   
 When  $x = 0, y = -2$   
 Draw a broken line in Quadrant 4.  
 Use  $(0, 0)$  as a test point.  
 L.S. =  $0$ ; R.S. =  $6$   
 Since  $0 < 6$ , the origin lies in the shaded region.  
 Shade the region above the line.

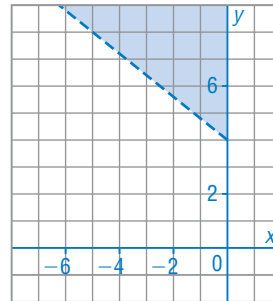
Graph of  $2x - 3y < 6$ ,  
 $x \geq 0, y \leq 0$



c)  $4x + 5y - 20 > 0$ ; for  $x \leq 0, y \geq 0$

Since  $x \leq 0, y \geq 0$ , the graph is in Quadrant 2.  
 Graph the related function.  
 When  $x = 0, y = 4$   
 When  $x = -5, y = 8$   
 Draw a broken line in Quadrant 2.  
 Use  $(0, 0)$  as a test point.  
 L.S. =  $-20$ ; R.S. =  $0$   
 Since  $-20 < 0$ , the origin does not lie in the shaded region.  
 Shade the region above the line.

Graph of  $4x + 5y - 20 > 0$ ,  
 $x \leq 0, y \geq 0$



**14. a)** For  $A(9, a)$  to be a solution of  $3x - 2y < 5$ , what must be true about  $a$ ?

Substitute the coordinates of A in the inequality.  
 $3(9) - 2(a) < 5$  Solve for  $a$ .  
 $2a > 22$   
 $a > 11$

b) For  $B(b, -3)$  to be a solution of  $3x + 4y \geq -12$ , what must be true about  $b$ ?

Substitute the coordinates of B in the inequality.  
 $3(b) + 4(-3) \geq -12$  Solve for  $b$ .  
 $3b \geq 0$   
 $b \geq 0$

15. A personal trainer books clients for either 45-min or 60-min appointments. He meets with clients a maximum of 40 h each week.

- a) Write an inequality that represents the trainer's weekly appointments.

Let  $x$  represent the number of 45-min appointments and  $y$  represent the number of 60-min appointments.

An inequality is:  $45x + 60y \leq 2400$

Divide by 15.

$3x + 4y \leq 160$

- b) Graph the related equation, then describe the graph of the inequality.

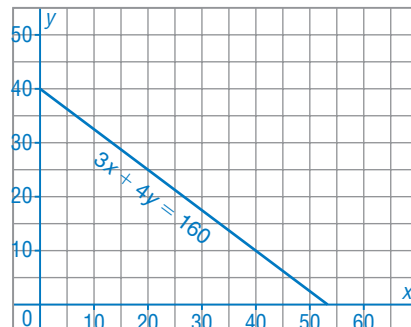
Determine the coordinates of 2 points that satisfy the related function.

When  $x = 0$ ,  $y = 40$

When  $x = 20$ ,  $y = 25$

Join the points with a solid line.

The solution is the points, with whole-number coordinates, on and below the line.



- c) How many 45-min appointments are possible if no 60-min appointments are scheduled? Where is the point that represents this situation located on the graph?

For no 60-min appointments,  $y = 0$ , so the point is on the  $x$ -axis; it is the point with whole-number coordinates that is closest to the  $x$ -intercept of the graph of the related equation. When  $y = 0$ ,

$$x = \frac{2400}{45}, \text{ or } 53.\bar{3}$$

Fifty-three 45-min appointments are possible.

16. Graph this inequality. Identify the strategy you used and explain why you chose that strategy.

$$\frac{x}{3} + \frac{y}{2} \geq 1$$

Graph the related function.

Determine the intercepts.

When  $y = 0$ ,  $x = 3$

When  $x = 0$ ,  $y = 2$

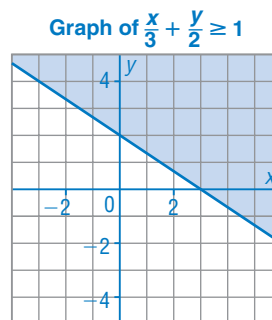
Draw a solid line.

Use  $(0, 0)$  as a test point.

L.S. = 0; R.S. = 1

Since  $0 < 1$ , the origin is not in the shaded region.

Shade the region above the line.





**C**

- 17.** How is a linear inequality in two variables similar to a linear inequality in one variable? How are the inequalities different?

The solutions of both inequalities are usually sets of values. A linear inequality in one variable is a set of numbers that can be represented on a number line. A linear inequality in two variables is a set of ordered pairs that can be represented on a coordinate plane.